Progress report of the APEC project:
“Collaborative Studies on Innovations for Teaching and Learning Mathematics in Different Cultures (II) - Lesson Study focusing on Mathematical Thinking -”

Center for Research on International Cooperation in Educational Development (CRICED)
University of Tsukuba
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