



*Progress report of the APEC project:
"Collaborative Studies on Innovations for Teaching
and Learning Mathematics in Different Cultures (II)
- Lesson Study focusing on Mathematical Thinking -"*



*Center for Research on International Cooperation
in Educational Development (CRICED)*



University of Tsukuba

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CONTENTS

PREFACE	1
INTRODUCTION	5
CONCLUSION	15
APEC SYMPOSIUM: 3-4 DECEMBER 2006	27
GREETING ADDRESS	
YUTAKA TSUJINAKA (Vice president of the University of Tsukuba)	31
YUKITSUGU ONO (Deputy Director for International Affairs Division, Minister's Secretariat, of the Ministry of Education, Culture, Sports, Science and Technology).....	33
SHINICHI ISHIHARA (Team Director, Basic Education Team II, Group I (Basic Education), Human Development Department, the Japan International Cooperation Agency)	34
SHIZUMI SHIMIZU (Vice President of the Japan Society of Mathematics Education).....	35
Program	37
⊙ What is mathematical thinking and why is it important?	39
Kaye Stacey (Australia)	
⊙ Encouraging mathematical thinking that has both power and simplicity	49
David Tall (UK)	
⊙ Designing mathematics conjecturing activities to foster thinking and constructing actively.....	65
Fou Lai Lin (Chinese Taipei)	
⊙ Developing mathematical thinking in Singapore elementary schools.....	75
Yeap Ban Har (Singapore)	
⊙ Promoting mathematical thinking in the Malaysian classroom: issues and challenges	81
Lim Chap Sam & Hwa Tee Yong (Malaysia)	
⊙ Enhancing elementary school mathematics teachers' mathematical thinking through in-service training	91
Soledad A. Ulep (Philippines)	
⊙ Mathematical thinking and how to teach it.....	105
Shigeo Katagiri (Ex professor of the Yokohama National University, Japan)	

APEC CONFERENCE: SPECIALIST SESSION, 5-7 DECEMBER 2006 159

Program 161

- ⊙ Developing mathematical reasoning through argumentation 163
Peter Gould (Australia)
- ⊙ Mathematical Thinking in Brunei curriculum: implementation issues and challenges 169
Madihah Khalid (Brunei Darussalam)
- ⊙ Lesson study: promoting student thinking on the concept of least common multiple (LCM) through realistic approach in the 4th grade of primary mathematics teaching 179
Marsigit, Atmini Dhoruri, Sugiman and Ali Mahmudi (Indonesia)
- ⊙ Developing mathematical thinking in classroom 193
Masami Isoda (Japan)
- ⊙ Mathematical thinking from the perspectives of problem solving and area of learning contents 237
Kazuyoshi Okubo (Japan)
- ⊙ Perspectives on mathematical thinking in Korea 245
Inchul Jung (Korea)
- ⊙ Developing student's mathematical thinking through lesson study in Thailand.... 255
Maitree Inprasitha and Suladda Loipha (Thailand)
- ⊙ Developing mathematical thinking through problem-based lessons..... 265
Soledad A. Ulep (Philippines)
- ⊙ Developing mathematical thinking through lesson study: overcoming barriers to effective implementation 275
Patsy Wang-Iverson (USA)
- ⊙ Mathematical thinking in primary school and junior high school 291
Shangzhi Wang, Dan Zhang and Siming Zhang (China)
- ⊙ Some remarks on mathematical thinking in education 297
Chang-Shou Lin and Su-Chun Lin (Chinese Taipei)
- ⊙ Development of mathematical thinking in Hong Kong schools 301
Cheng Chun Chor Litwin (Hong Kong)
- ⊙ Mexican perspective on mathematical thinking 311
Tenoch Cedillo and Marcela Santillan (Mexico)
- ⊙ Mathematical thinking like angular stone in the understanding of real world phenomena..... 317
Mag. Francisco Cerda Bonomo (Chile)
- ⊙ Using lesson study to implement more effective lessons: focusing on mathematical thinking 329
Tran Vui (Vietnam)

◎ Study lessons in Attached Elementary School of the University of Tsukuba, Hokuto Elementary School, and Maruyama Elementary School	339
APPENDIX: RELATED DOCUMENTS.....	361