



On Modeling

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What is Modeling?

Why Modeling?

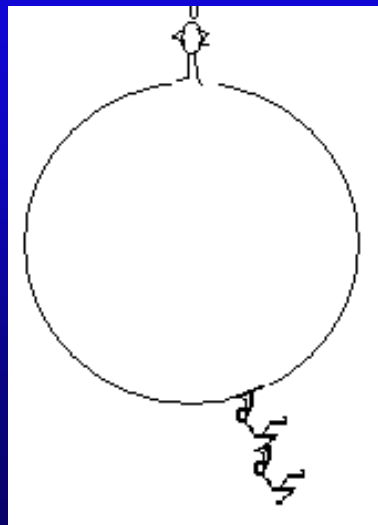
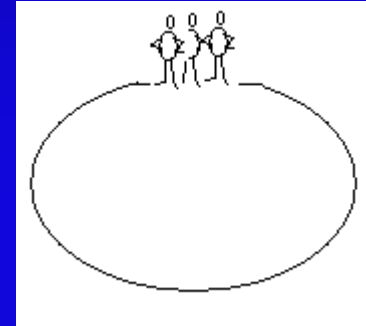
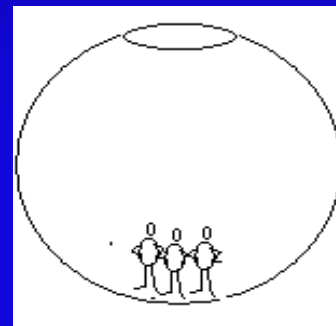
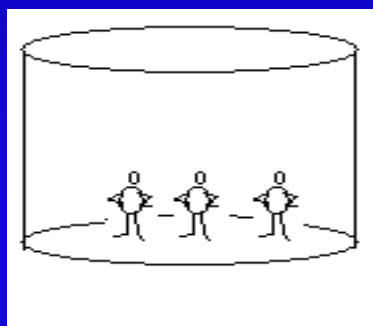
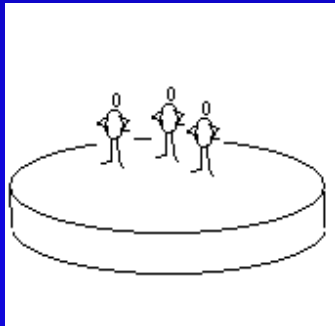
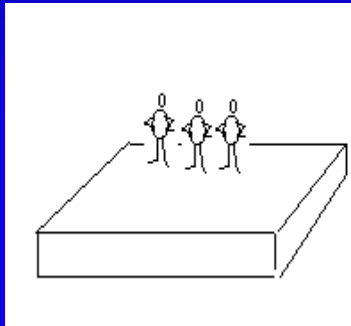
How to teach Modeling?

What is Modeling?

Why Modeling?

How to teach Modeling?

What is Modeling?



Predictions

Explanations

Implicit versus Explicit Models

Particulate model of matter

Wave model of matter

Poblational model of life

Informational model of life

Hydraulic model of mind

Computational model of mind

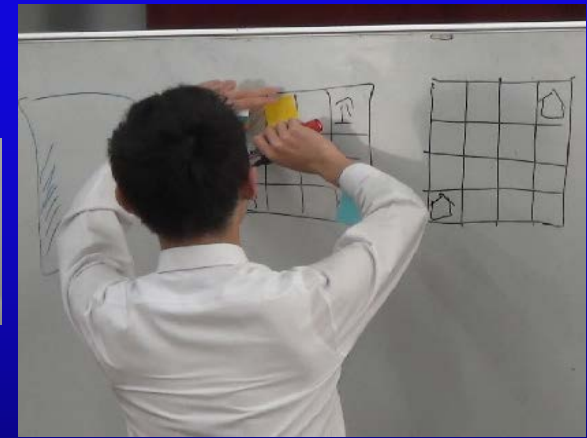
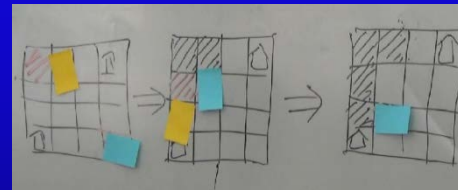
Network model of mind

Concrete

Pictoric

Symbolic

Transit from concrete models to symbolic models



What is Mathematical Modeling?

Explicit

Symbolic

Expressed in mathematical language

What is Modeling?

Why Modeling?

How to teach Modeling?

Why Explicit Models?

Compare

Improve

Predictions

Explanations

Why Mathematical Modeling?

More powerful

Predictions in new situations

Explanations in new situations

Hidden mechanisms

Why Mathematical Modeling?

Critical skill for XXI century

Citizens have to deal with

- more info from devices and the cloud

- more complex information

- more multidisciplinary information

- more complex decisions

Credit risk

Insurance

Retail

Customer support

Machine maintenance

Process monitoring

Medical diagnosis

Autonomous navigation systems

Personal assistants

FUEGO - U.C. Berkeley



Common Core v/s NGSS

Mathematical Practices

1. Make sense of problems and persevere in solving them
2. Reason abstractly and quantitatively
3. Construct viable arguments and critique the reasoning of others
4. **Model with mathematics**
5. Use appropriate tools strategically
6. Attend to precision
7. Look for and make use of structure
8. Looking for and expressing regularity in repeated reasoning

Scientific and Engineering Practices

1. Ask questions and define problems
2. **Develop and use models**
3. Plan and carry out investigations
4. Analyze and interpret data
5. Use mathematics and computational thinking
6. Construct explanations and design solutions
7. Engage in argument from evidence
8. Obtain, evaluate, and communicate information

What is Modeling?

Why Modeling?

How to teach Modeling?

How to teach Modeling?

1) Use-Select-Adjust-Build



00:00:19 0 100

Bug always move to the neighbor cell with more food until there is no neighbor cell with more food.

Connect the blue cell. Then continue consecutively connecting the cells that Bugy will visit.



11	17	21	21	22	23	21	22	22	17
10	17	22	27	28	29	26	28	20	17
10	16	21	29	33	34	33	29	23	18
11	16	24	27	34	40	33	28	23	18
10	15	24	28	33	33	26	30	21	15
9	16	20	28	27	27	29	29	22	18
10	15	22	24	21	22	20	21	23	17
9	15	16	18	16	18	15	15	16	15
12	10	10	10	11	11	9	11	11	10
1	3	5	2	6	5	3	3	3	2



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11	16	24	27	34	40	33	28	23	18
10	15	24	28	33	33	26	30	21	15
9	16	20	28	27	27	29	29	22	18
10	15	22	24	21	22	20	21	23	17
9	15	16	18	16	18	15	15	16	15
12	10	10	10	11	11	9	11	11	10
1	3	5	2	6	5	3	3	3	2



Landslides



La roca siempre se mueve a la celda vecina de menor altura, y así lo hará hasta que no pueda descender más.

Conecta la posición inicial de la roca, que es la celda con más altura.

Luego consecutivamente conecta las celdas donde la roca pasará, y determina si chocará con la casa de Ana que es la celda roja.



16	17	21	21	22	23	21	22	22	17
10	17	22	27	28	29	26	28	20	17
10	16	21	29	39	34	36	29	23	18
11	16	24	27	34	40	39	28	23	18
10	16	24	28	33	34	34	30	21	15
11	16	20	21	27	34	29	29	22	18
10	15	22	24	21	22	20	21	23	17
9	15	16	8	16	18	15	15	16	15
12	10	11	11	11	11	9	11	11	10
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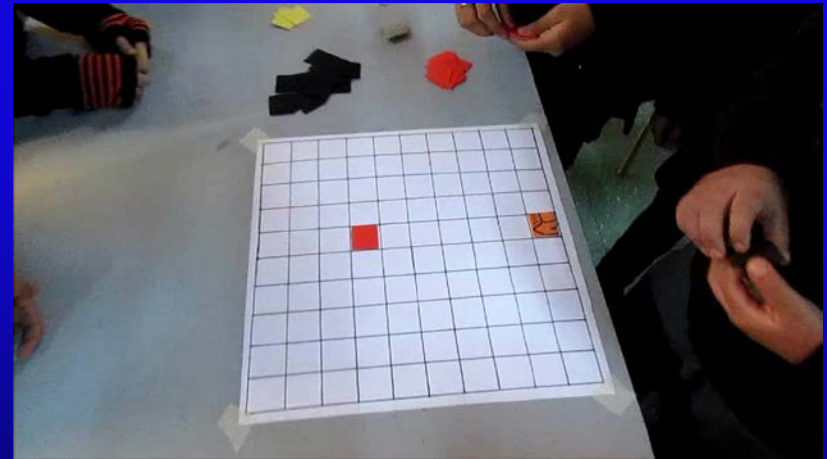
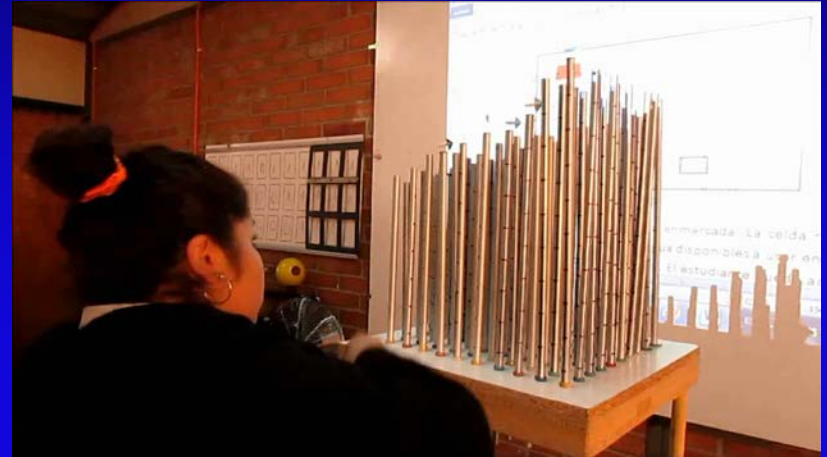
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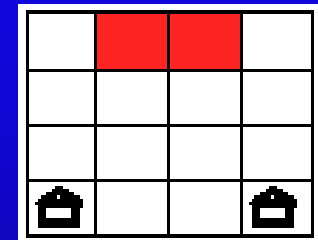
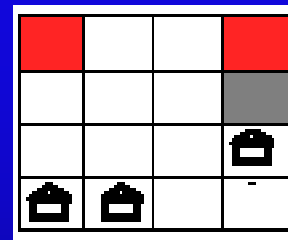
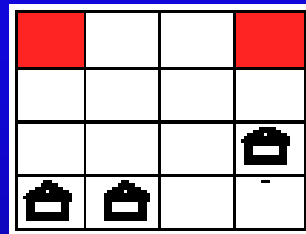
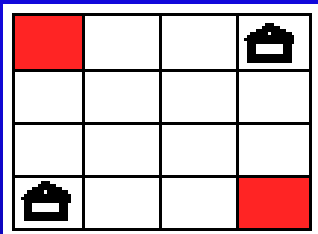
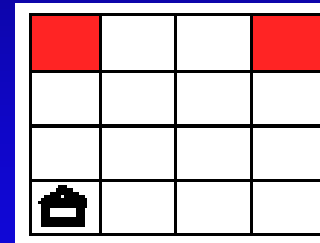
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How to teach Modeling?

2) Concrete Model → Pictorial Model → Math Model



Program an autonomous drone



Fuego - U.C. Berkeley

How to teach Modeling?

3) Predict & explain

Teacher presents a challenge



Students:

Teacher track
answers in real time

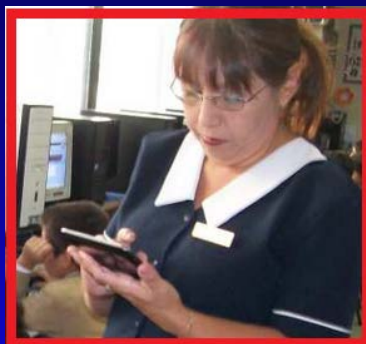
Make predictions

Explain predictions with models

Make experiment

Explain agreement with models

Peer review



Respuestas de los alumnos

Número de estudiantes que respondieron: 11 de 3 estudiantes conectados.

Hora (HH:MM:SS)	Nombre	RUT	Respuesta	
09:32:29	 Rain A, Elmer	20789738-8	si porque el baso con el agua hela se pone mas oscura por la poca energia que tiene, con el agua caliente tiene mas energia que hace que la tinta se disuelva mas rapido	Premiar con 4 banderas
09:33:26	 Pradenas B, Christopher	20446681-5	concuerdan con un poco de lo que dije me falto decir que tambien cambia un poco de color y estaba bien que se disuelve mas rapido en el agua caliente	Premiar con 4 banderas
09:34:19	 Cid M, Jairo	20813352-7	si por que la tinta en el recipiente con agua caliente se disolvio mas rapido que el que tenia agua fria	Premiar con 4 banderas
09:35:27	 Rain A, Elmer	20450148-3	en el transcurso de los dos minutos el recipiente de agua helada se demoro mas en disolverse y de agua caliente se	Premiar con 4 banderas



Peers Review

Visualize thinking of students' peers

13:03:09	 Bascur G, Cris	21797658-8	Saez V, Catalina dijo: porque ella dice que tiene 30 panes y despues dice que les corresponde a cada uno 180 y esta mal y 30 es menor que (180) tenia que dividir 180 dividido en 30	NOPOOOOOO SI ERA KE RRESPONDER 30DIVIDIDO EN 6	4 b
13:03:09	 Fernández C, Johan	22037069-0	Carrasco F, Thiare dijo: esta mal por que dijo que tenia que aver 180 panes dijo ella	mal	Premiar con 4 banderas
13:03:56	 Sánchez M, Carla	21818369-7	Sánchez M, Carla dijo: estamal porque dibidio y es multiplicar	esta mal	Premiar con 4 banderas

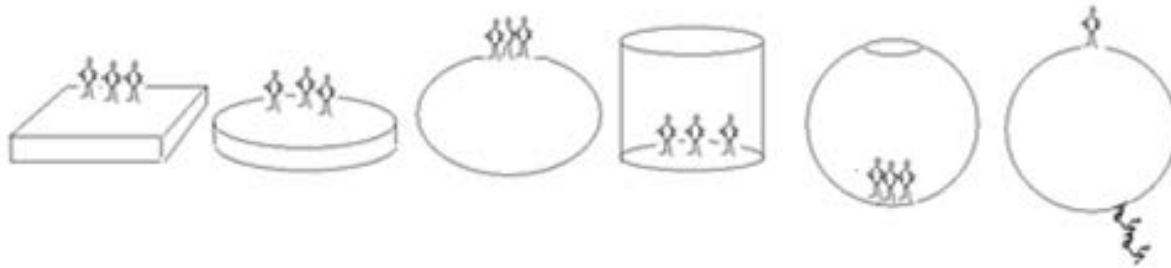


Peers commentary

Record on the cloud each prediction and each explanation of every student

→ Powerful data mining

→ Critical information to improve practices



PLANET-STEM

Paradigm-shifting Learning And Networking for Education using Technology
for Science Technology Engineering Mathematics (STEM)

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Educator and Research Physicist
University of California, Berkeley



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Educator and STEM Researcher
CIAE, University of Chile



www.planet-stem.org

How to teach Modeling?

4) Inter classroom competition
and
Intra class collaboration

Inter school on-line synchronous tournaments



Classroom n



Classroom k

Conectado a sala 6

Roberto

Hola, en este juego puedes hacer clic en cualquier celda para llegar a tu destino. Haz clic en el tablero para eliminar estos mensajes.

Jugada N°1

Roberto

Finalizar turno

Haz girar la tómbola...

Turno N°1

105 s

Oro:0 Err:0

10

Esperando turno...

Turno N°0

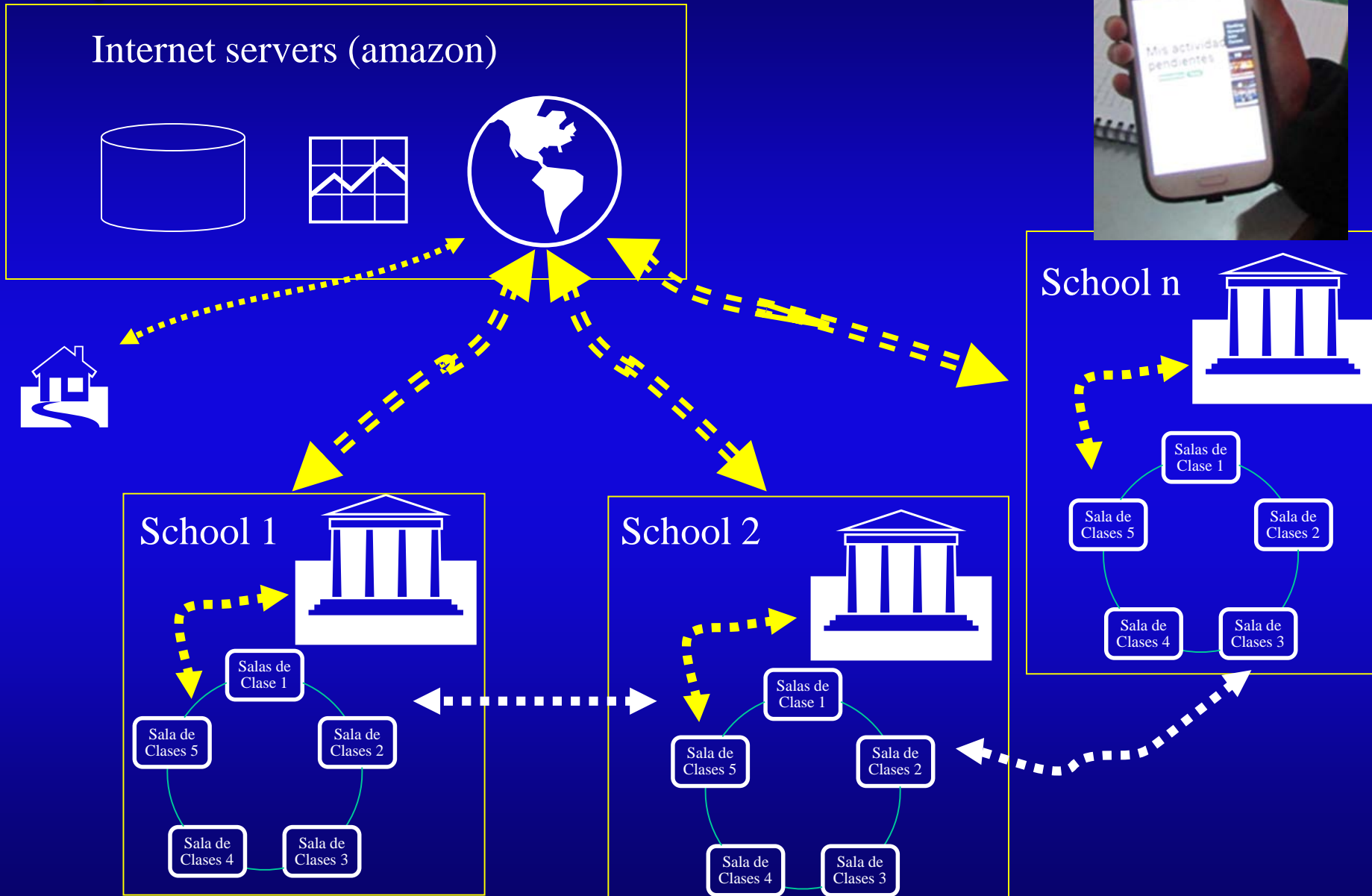
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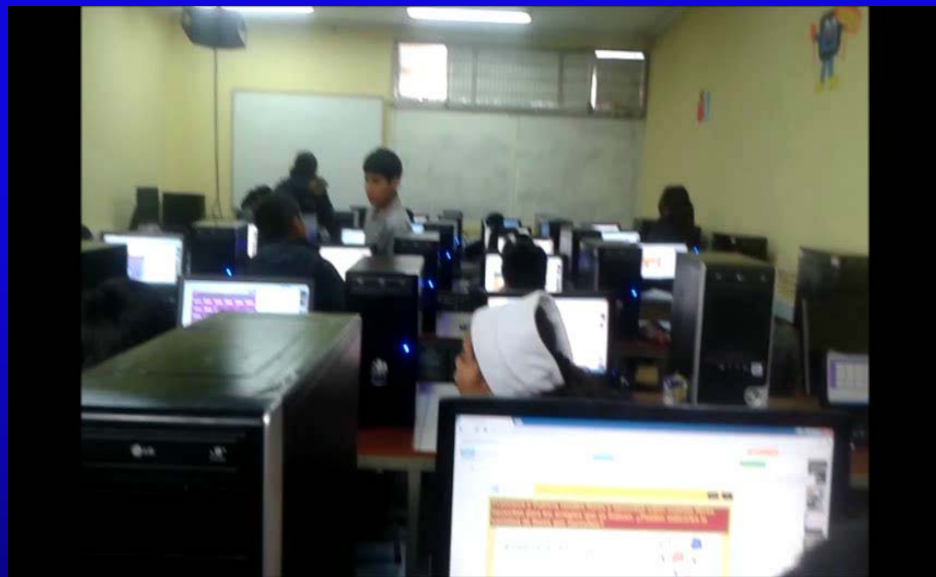
¿...?

Contar de nuevo...



Synchronized classrooms





How to teach Modeling?

- 1) Use-Select-Adjust-Build
- 2) Concrete Model → Pictorial Model → Math Model
- 3) Predict & explain (visualize with models)
- 4) Inter classroom competition & Intra class collaboration

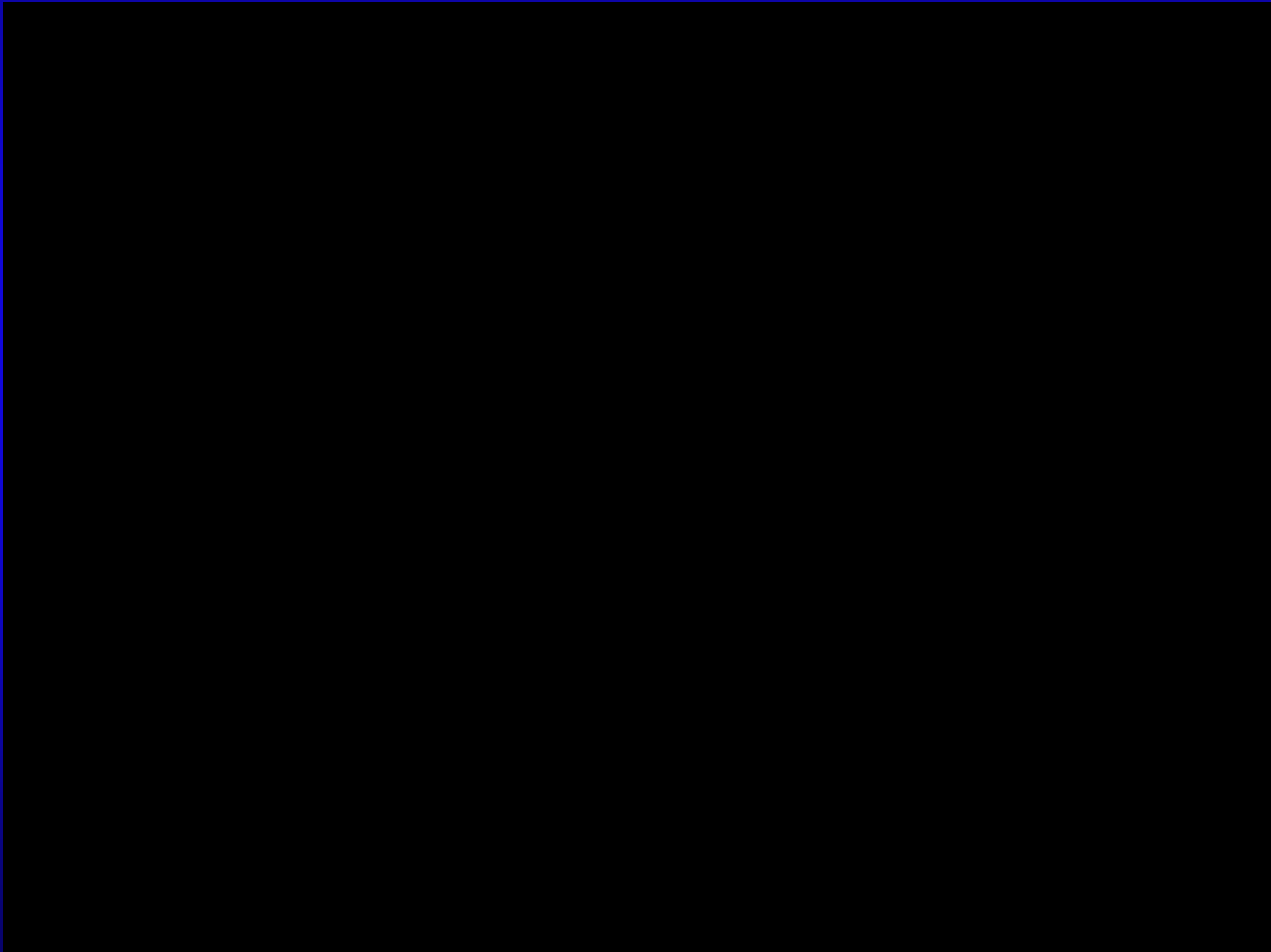
Homework

Energy?

Energy efficiency?

Energy efficiency in Mining and
in Industry?

Can we explain why it works?



Isn't there beauty here?

It sparked the whole industrial revolution

How to scale this process to the whole school system?

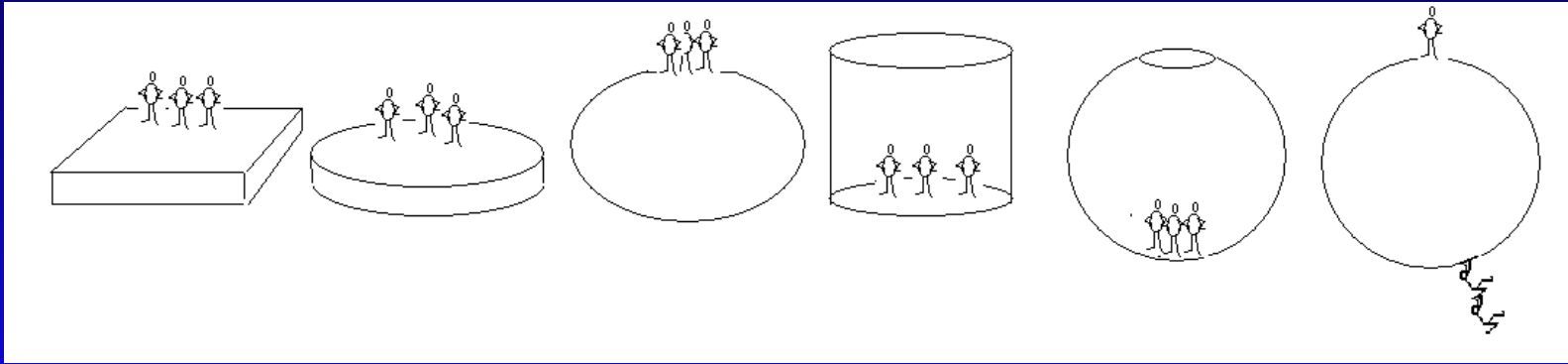


Lesson study and public classes

What is Modeling?

Why Modeling?

How to teach Modeling?



www.planet-stem.org

Thank you